

Pic. No. _____

Mathematics Part-I

SECTION "A"

Pic. No. _____

Time: 20 Min

Marks: 20

NOTE: Use this sheet for this section. No marks will be awarded for cutting, erasing or overwriting.

Q1. Choose the correct answer from the given choices i.e. (a, b, c, d) and insert into the relevant box.

- | | |
|---|---|
| <p>(i). $(-i)^{-19} =$ _____.</p> <p>(A) i (B) $-i$ (C) 1 (D) -1</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(ii). A group G is called abelian group if it has _____.</p> <p>(A) Distributive prop (B) Associative prop (C) Commutative prop (D) Identity</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(iii). If $z = a + ib$ then $\frac{z}{z} =$ _____.</p> <p>(A) $a^2 - b^2$ (B) $a^2 + b^2$ (C) $\sqrt{a^2 + b^2}$ (D) $\sqrt{a^2 - b^2}$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(iv). If A is a square Matrix and $A = 0$ the $a^{-1} =$ _____.</p> <p>(A) A (B) $\frac{1}{ A } adjA$ (C) Not exist (D) $-A$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(v). If A is a square Matrix of order n the cofactor of the element a_{ij} i.e $A_{ij} =$ _____.</p> <p>(A) $(-1)^{i+j} M_{ij}$ (B) M_{ij} (C) $-M_{ij}$ (D) $(-1)^{i+i} M_{ij}$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(vi). The equation $4x^2 + x + 1 = 0$ has _____ roots.</p> <p>(A) Real (B) Imaginary (C) Complex (D) None</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(vii). $\omega^{-5} =$ _____. Where ω is a cube root of unity.</p> <p>(A) 1 (B) 0 (C) ω (D) ω^2</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(viii). If the roots of the quadratic equation are rational then _____.</p> <p>(A) $b^2 - 4ac = 0$ (B) $b^2 - 4ac > 0$ (C) $b^2 - 4ac \geq 0$ (D) $b^2 - 4ac < 0$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(ix). If $a_n = (-1)^n(n+1)$ then $a_3 =$ _____.</p> <p>(A) 3 (B) -4 (C) 4 (D) 2</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(x). True relation between Arithmetic Geometric and Harmonic Means is _____.</p> <p>(A) $A > H > G$ (B) $G > H > A$ (C) $H > G > A$ (D) $A > G > H$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xi). $1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots$ is the series of _____.</p> <p>(A) Arithmetic (B) Geometric (C) Harmonic (D) Neither of them</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xii). ${}^nC_r =$ _____.</p> <p>(A) $\frac{1}{r!} \frac{P}{r}$ (B) $\frac{P}{r}$ (C) $\frac{C}{r}$ (D) $\frac{C}{r-1}$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xiii). In the binomial expansion of $(a+b)^n$ the number of terms are _____.</p> <p>(A) $n+2$ (B) $n+1$ (C) n (D) $n-1$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xiv). $\frac{-3\pi}{4}$ radians = _____.</p> <p>(a) 130° (b) -135° (c) 135° (d) $\frac{180}{\pi}$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xv). $\cos(\alpha + \frac{\pi}{2}) =$ _____.</p> <p>(A) $\cos \alpha$ (B) $-\cos \alpha$ (C) $\sin \alpha$ (D) $-\sin \alpha$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xvi). Period of $5 \sin 3x$ is _____.</p> <p>(A) 2π (B) $\frac{3\pi}{2}$ (C) π (D) $\frac{2\pi}{3}$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xvii). In law of tangents $\frac{a+c}{a-c} =$ _____.</p> <p>(A) $\tan(\frac{\alpha+\beta}{2})$ (B) $\frac{\tan(\frac{\alpha+y}{2})}{\tan(\frac{\alpha-y}{2})}$ (C) $\tan(\frac{\beta-y}{2})$ (D) $\frac{\tan(\frac{\alpha-y}{2})}{\tan(\frac{\alpha+y}{2})}$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xviii). A circle drawn inside a triangle and touching the sides of a triangle is called _____.</p> <p>(A) In Circle (B) Circum Circle (C) Escribe Circle (D) None of these</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xix). Domain of $y = \sec x$ is _____.</p> <p>(a). $[0, \pi]$ (b). $[-\pi, \pi]$ (c). $(-2\pi, 2\pi)$ (d). $[0, \pi] - \frac{\pi}{2}$</p> | <input style="width: 80px; height: 30px;" type="text"/> |
| <p>(xx). $\cos^{-1}(-x) =$ _____.</p> <p>(a). $\pi - \cos^{-1}x$ (b). $\pi + \cos^{-1}x$ (c). $\cos^{-1}x$ (d). $-\cos^{-1}x$</p> | <input style="width: 80px; height: 30px;" type="text"/> |

Mathematics Part-I

Time: Allowed: 2.40h

Marks: 80

SECTION "B"

Marks: 50

Q2. Answer any Ten (10) of the following Parts.

- (i) if $Z_1 = a + ib$, $Z_2 = c + id$ then prove that $\left[\frac{\overline{Z_1}}{Z_2} \right] = \frac{\overline{Z_1}}{Z_2}$
- (ii) $S = \{0, 1, 2, 3\}$ show that $(S, +)$ is a Semi group. Where $+$ defines addition Modulo 4.
- (iii) Find the inverse of the Matrix $\begin{bmatrix} 4 & -2 & 5 \\ 2 & 1 & 0 \\ -2 & 2 & 3 \end{bmatrix}$ by using elementary row operation.
- (iv) Solve the equation $(x-3)(x+9)(x+5)(x-7) = 385$
- (v) If α, β are the roots of $x^2 - 4x + 2 = 0$ then find the equation whose roots are $\alpha + \frac{1}{\alpha}, \beta + \frac{1}{\beta}$
- (vi) Decompose $\frac{x^2 + 3}{(x-1)(x^2+1)^2}$ into Partial fraction.
- (vii) Find four numbers in A.P such that their sum is 66 and the sum of their squares is 1214.
- (viii) Find the Sum to n terms of the series $2.3.1 + 3.4.4 + 4.5.7 + \dots$
- (ix) Find the value of n when ${}^n P_4 : {}^{n-1} P_3 = 9:1$
- (x) Prove by Mathematical Indus that $2^2 + 4^2 + 6^2 + \dots + (2n)^2 = \frac{2}{3}n(n+1)(2n+1)$
- (xi) Prove that $\frac{\sin x - \cos x}{\tan^2 x - 1} = \frac{\cos^2 x}{\sin x - \cos x}$
- (xii) Show that $\sin 5\theta + 2 \sin 3\theta + \sin \theta = 4 \sin 3\theta \cos^2 \theta$
- (xiii) Use the law of cosines to prove that $1 + \cos \alpha = \frac{(b+c+a)(b+c-a)}{2bc}$

SECTION "C"

Marks: 30

Note: Attempt any THREE questions. All questions carry equal marks.

- Q3. (A) Find real and imaginary Parts of $\left(\frac{1-i\sqrt{3}}{1+i\sqrt{3}} \right)^4$ (B) Solve the Matrix equation for x
- $$x \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix} - \begin{bmatrix} 3 & 2 \\ 2 & 1 \end{bmatrix} = \begin{bmatrix} -1 & 3 \\ 4 & 5 \end{bmatrix}$$

- Q4. (A) if $n+1$, and $x-2$ are the factors of the polynomial $x^3 - mx^2 + nx + 2$ then using synthetic division to find the values of m & n.

- (B) If $\frac{1}{y-x}, \frac{1}{2y}$ and $\frac{1}{y-z}$ from an A.P. prove that x, y and z form a G.P.

- Q.5 (A) Find the term independent of x in the expansion of $\left(\sqrt{x} + \frac{1}{3x} \right)^{10}$
- (B) If $y = \frac{1}{2^2} + \frac{1.3}{2!} \cdot \frac{1}{2^4} + \frac{1.3.5}{3!} \cdot \frac{1}{2^6} + \dots$ then $y^2 + 2y - 1 = 0$

- Q.6 (A) Prove $\sin^2 \frac{\theta}{2} = \frac{\sin \theta \cdot \tan \frac{\theta}{2}}{2}$

- (B) The angle of elevation of a building is 48° from A and 61° from B. if AB is 20 m. Find the height of the building.