



FEDERAL PUBLIC SERVICE COMMISSION
 COMPETITIVE EXAMINATION FOR
 RECRUITMENT TO POSTS IN BPS-17 UNDER
 THE FEDERAL GOVERNMENT, 2010

Roll Number

APPLIED MATH, PAPER-II

TIME ALLOWED: 3 HOURS

MAXIMUM MARKS:100

NOTE:

- (i) Attempt **FIVE** question in all by selecting at least **TWO** questions from **SECTION-A**, **ONE** question from **SECTION-B** and **TWO** questions from **SECTION-C**. All questions carry **EQUAL** marks.
 (ii) **Use of Scientific Calculator is allowed.**

SECTION – A

- Q.1.** Solve the following equations:
 (a) $d^2y/dx^2 + 5 dy/dx + 6y = x$ (10)
 (b) $d^2y/dx^2 + 5 y x = e^x$ (10)
- Q.2.** (a) Derive Cauchy Riemann partial differential equations. (10)
 (b) Derive Laplace Equation. (10)
- Q.3.** Solve:
 (a) $(\partial^2 / \partial x^2 + \partial^2 / \partial x \partial y + \partial^2 / \partial y^2) u = 4 e^{3y}$ (10)
 (b) $u'' + 6u' + 9 = 0$; Given that $u(0)=2$ and $u'(0)=0$. (10)

SECTION – B

- Q.4.** (a) Discuss the following supported by examples:
 • Tensor, (5)
 • $\epsilon_{ijk} \epsilon_{lmk}$ (5)
 • Scalar Fields for a continuously differentiable function $f=f(x,y,z)$ (5)
 (b) Can we call a vector as Tensor, discuss.
 What is difference between a vector and a tensor?
 What happens if we permute the subscripts of a tensor? (5)
- Q.5.** (a) Discuss the simplest and efficient method of finding the inverse of a square matrix a_{ij} of order 3×3 . (10)
 (b) Apply any efficient method to compute the inverse of the following matrix A: (10)

$$A = \begin{bmatrix} 25 & 2 & 1 \\ 2 & 10 & 1 \\ 1 & 1 & 4 \end{bmatrix}$$

SECTION – C

- Q.6.** (a) Develop Gauss Seidel iterative Method for solving a linear system of equations $Ax = b$, where A is the coefficient matrix. (10)
 (b) Apply Gauss Seidel iterative Method to solve the following equations: (10)
 $25X_1 + 2X_2 + X_3 = 69$
 $2X_1 + 10X_2 + X_3 = 63$
 $X_1 + 2X_2 + X_3 = 43$
- Q.7.** (a) Derive Simpson's Rule for finding out the integral of a function $f(x)$ from limits $x=a$ to $x=b$ for $n=6$ subintervals (i.e. steps). (10)
 (b) Apply Simpson's Rule for $n=6$ to evaluate: (10)
 $\int_0^1 f(x) dx$ where $f(x) = 1/(1+x^2)$.
- Q.8.** (a) Derive Lagrange Interpolation Formula for 4 points: (10)
 (b) A curve passes through the following points: (10)
 $(0,1), (1,2), (2,5), (3,10)$. Apply this Lagrange Formula to interpolate the polynomial.